

# Package ‘swash’

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**Type** Package

**Title** Swash-Backwash Model for the Single Epidemic Wave

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**Depends** R (>= 3.5.0), lubridate, sf, spdep

**Description** The Swash-Backwash Model for the Single Epidemic Wave was developed by Cliff and Haggett (2006) <[doi:10.1007/s10109-006-0027-8](https://doi.org/10.1007/s10109-006-0027-8)> to model the velocity of spread of infectious diseases across space. This package enables the calculation of the Swash-Backwash Model for user-supplied panel data on regional infections. The package also provides additional functions for bootstrap confidence intervals, country comparison, visualization of results, and data management.

**License** GPL (>= 2)

**Imports** methods

**NeedsCompilation** no

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swash-package	<i>Implementation of the Swash-Backwash Model for the Single Epidemic Wave and additional functions in R</i>
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## Description

Swash-Backwash Model for the single epidemic wave (Cliff and Haggett 2006) with additional functions for bootstrap confidence intervals and data management; other functions for spatio-temporal analysis and modeling of infectious diseases

## Details

The Swash-Backwash Model for the Single Epidemic Wave is the spatial equivalent of the classic epidemiological SIR (Susceptible-Infected-Recovered) model. It was developed by Cliff and Haggett (2006) to model the velocity of spread of infectious diseases across space. Current applications can be found, for example, in Smallman-Raynor et al. (2022a,b). This package enables the calculation of the Swash-Backwash Model for user-supplied panel data on regional infections. The core of this is the `swash()` function, which calculates the model and creates a model object of the `sbm` class defined in this package. This class can be used to visualize results (`summary()`, `plot()`) and calculate bootstrap confidence intervals for the model estimates (`confint(sbm)`). The package also contains other functions for spatio-temporal analysis and modeling of infectious diseases, such as fitting logistic growth models (`growth(sbm)`, `logistic_growth()`) and exponential growth models for the initial phase of a spread (`growth_initial(sbm)`, `exponential_growth()`), as well as for spatial statistics.

**Author(s)**

Thomas Wieland

**References***Swash-Backwash Model:*

Cliff AD, Haggett P (2006) A swash-backwash model of the single epidemic wave. *Journal of Geographical Systems* 8(3), 227–252. doi:10.1007/s1010900600278

Smallman-Raynor MR, Cliff AD, Stickler PJ (2022a) Meningococcal Meningitis and Coal Mining in Provincial England: Geographical Perspectives on a Major Epidemic, 1929–33. *Geographical Analysis* 54, 197–216. doi:10.1111/gean.12272

Smallman-Raynor MR, Cliff AD, The COVID-19 Genomics UK (COG-UK) Consortium (2022b) Spatial growth rate of emerging SARS-CoV-2 lineages in England, September 2020–December 2021. *Epidemiology and Infection* 150, e145. doi:10.1017/S0950268822001285.

*Basics of epidemiological modeling:*

Bonifazi G et al. (2021) A simplified estimate of the effective reproduction number  $R_t$  using its relation with the doubling time and application to Italian COVID-19 data. *The European Physical Journal Plus* 136, 386. doi:10.1140/epjp/s13360021013396

Chowell G, Simonsen L, Viboud C, Yang K (2014) Is West Africa Approaching a Catastrophic Phase or is the 2014 Ebola Epidemic Slowing Down? Different Models Yield Different Answers for Liberia. *PLoS currents* 6. doi:10.1371/currents.outbreaks.b4690859d91684da963dc40e00f3da81

Li, MY (2018) An Introduction to Mathematical Modeling of Infectious Diseases. doi:10.1007/9783319721224

Nishiura H, Chowell G (2009) The effective reproduction number as a prelude to statistical estimation of time-dependent epidemic trends. In Chowell G, Hyman JM, Bettencourt LMA (eds.) *Mathematical and statistical estimation approaches in epidemiology*, 103–121. doi:10.1007/97890-48123131\_5

Pell B, Kuang Y, Viboud C, Chowell G (2018) Using phenomenological models for forecasting the 2015 ebola challenge. *Epidemics* 22, 62–70. doi:10.1016/j.epidem.2016.11.002

Wieland T (2020) A phenomenological approach to assessing the effectiveness of COVID-19 related nonpharmaceutical interventions in Germany. *Safety Science* 131, 104924. doi:10.1016/j.ssci.2020.104924

*Spatio-temporal analysis and modeling of infectious diseases:*

Bourdin S, Jeanne L, Nadou F, Noiret G (2021) Does lockdown work? A spatial analysis of the spread and concentration of Covid-19 in Italy. *Regional Studies*, 55, 1182–1193. doi:10.1080/00343404.2021.1887471

Chowell G, Viboud C, Hyman JM, Simonsen L (2015) The Western Africa ebola virus disease epidemic exhibits both global exponential and local polynomial growth rates. *PLOS Currents Outbreaks*, ecurrents.outbreaks.8b55f4bad99ac5c5db3663e916803261. doi:10.1371/currents.outbreaks.8b55f4bad99ac5c5db36

Viboud C, Bjørnstad ON, Smith DL, Simonsen L, Miller MA, Grenfell BT (2006) Synchrony, Waves, and Spatial Hierarchies in the Spread of Influenza. *Science* 312, 447–451. doi:10.1126/science.1125237

Wieland T (2020) Flatten the Curve! Modeling SARS-CoV-2/COVID-19 Growth in Germany at the County Level. *REGION* 7(2), 43–83. doi:10.18335/region.v7i2.324

Wieland T (2022) Spatial patterns of excess mortality in the first year of the COVID-19 pandemic in Germany. *European Journal of Geography* 13(4), 18-33. doi:10.48088/ejg.t.wie.13.4.018.033

*Panel data:*

Greene, WH (2012) *Econometric Analysis*. Ch. 11.

Wooldridge, JM (2012) *Introductory Econometrics. A Modern Approach*. Ch. 13.

*Bootstrapping und bootstrap confidence intervals:*

Efron B, Tibshirani RJ (1993) *An Introduction to the Bootstrap*.

Ramachandran KM, Tsokos CP (2021) *Mathematical Statistics with Applications in R* (Third Edition). Ch. 13.3.1 (Bootstrap confidence intervals). doi:10.1016/B9780128178157.000130

## Examples

```
data(COVID19Cases_geoRegion)
# Get SWISS COVID19 cases at NUTS 3 level

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[!COVID19Cases_geoRegion$geoRegion %in% c("CH", "CHFL"),]
# Exclude CH = Switzerland total and CHFL = Switzerland and Liechtenstein total

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[COVID19Cases_geoRegion$datum <= "2020-05-31",]
# Extract first COVID-19 wave

CH_covidwave1 <-
  swash (
    data = COVID19Cases_geoRegion,
    col_cases = "entries",
    col_date = "datum",
    col_region = "geoRegion"
  )
# Swash-Backwash Model for Swiss COVID19 cases
# Spatial aggregate: NUTS 3 (cantons)

summary(CH_covidwave1)
# Summary of Swash-Backwash Model

plot(CH_covidwave1)
# Plot of Swash-Backwash Model edges and total epidemic curve
```

---

as\_balanced

*Correction of Non-balanced Panel Dataset with Regional Infection Data*

---

## Description

This function corrects non-balanced input panel data by replacing missing entries with a user-given constant (e.g., 0).

**Usage**

```
as_balanced(
  data,
  col_cases,
  col_date,
  col_region,
  fill_missing = 0
)
```

**Arguments**

data	data.frame with regional infection data
col_cases	Column containing the cases (numeric)
col_date	Column containing the time points (e.g., days)
col_region	Column containing the unique identifier of the regions (e.g., name, NUTS 3 code)
fill_missing	Constant to fill missing values (default and recommended: 0)

**Details**

The Swash-Backwash Model for the Single Epidemic Wave does not necessarily require balanced panel data in order for the calculations to be carried out. However, for a correct estimation it is implicitly assumed that the input data is balanced. The function corrects non-balanced panel data. It is executed automatically within the `swash()` function (when using the function `is_balanced()`), but can also be used separately.

**Value**

data	Corrected input dataset (data.frame)
------	--------------------------------------

**Author(s)**

Thomas Wieland

**References**

*Swash-Backwash Model:*

Cliff AD, Haggett P (2006) A swash-backwash model of the single epidemic wave. *Journal of Geographical Systems* 8(3), 227-252. doi:[10.1007/s1010900600278](https://doi.org/10.1007/s1010900600278)

Smallman-Raynor MR, Cliff AD, Stickler PJ (2022) Meningococcal Meningitis and Coal Mining in Provincial England: Geographical Perspectives on a Major Epidemic, 1929–33. *Geographical Analysis* 54, 197–216. doi:[10.1111/gean.12272](https://doi.org/10.1111/gean.12272)

Smallman-Raynor MR, Cliff AD, The COVID-19 Genomics UK (COG-UK) Consortium (2022) Spatial growth rate of emerging SARS-CoV-2 lineages in England, September 2020–December 2021. *Epidemiology and Infection* 150, e145. doi:[10.1017/S0950268822001285](https://doi.org/10.1017/S0950268822001285).

*Panel data:*

Greene, WH (2012) *Econometric Analysis*. Ch. 11.

Wooldridge, JM (2012) *Introductory Econometrics. A Modern Approach*. Ch. 13.

### See Also

[is\\_balanced](#)

### Examples

```
data(COVID19Cases_geoRegion)
# Get SWISS COVID19 cases at NUTS 3 level

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[!COVID19Cases_geoRegion$geoRegion %in% c("CH", "CHFL"),]
# Exclude CH = Switzerland total and CHFL = Switzerland and Liechtenstein total

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[COVID19Cases_geoRegion$datum <= "2020-05-31",]
# Extract first COVID-19 wave

COVID19Cases_geoRegion_balanced <-
  is_balanced(
    data = COVID19Cases_geoRegion,
    col_cases = "entries",
    col_date = "datum",
    col_region = "geoRegion"
  )
# Test whether "COVID19Cases_geoRegion" is balanced panel data

COVID19Cases_geoRegion_balanced$data_balanced
# Balanced? TRUE or FALSE

if (COVID19Cases_geoRegion_balanced$data_balanced == FALSE) {
  COVID19Cases_geoRegion <-
    as_balanced(
      COVID19Cases_geoRegion,
      col_cases = "entries",
      col_date = "datum",
      col_region = "geoRegion"
    )
}
# Correction of dataset "COVID19Cases_geoRegion"
# not necessary as parameter balance of is_balanced is set TRUE by default
```

---

compare\_countries

*Two-country Comparison of Swash-Backwash Model Parameters*

---

### Description

This function enables bootstrap estimates for the mean difference of Swash-Backwash Model parameters of two countries to be compared.

**Usage**

```
compare_countries(
  sbm1,
  sbm2,
  country_names = c("Country 1", "Country 2"),
  indicator = "R_0A",
  iterations = 20,
  samples_ratio = 0.8,
  alpha = 0.05,
  replace = TRUE
)
```

**Arguments**

sbm1	A sbm object for country 1
sbm2	A sbm object for country 2
country_names	list with user-given country names (two entries)
indicator	character, indicator to be analyzed ("S_A", "I_A", "R_A", "t_LE", "t_LE", or "R_0A" (default and recommended: "R_0A"))
iterations	Number of iterations for resampling (default: 100)
samples_ratio	Proportion of regions included in each sample (default: 0.8)
alpha	Significance level $\alpha$ for the confidence intervals (default: 0.05)
replace	Resampling with replacement (TRUE or FALSE, default: TRUE = bootstrap resampling)

**Details**

The combination of the Swash-Backwash Model and bootstrap resampling allows the estimation of mean differences of a user-specified model parameter (e.g., spatial reproduction number  $R_{OA}$ ) between two countries. This makes it possible to check whether the spatial spread velocity of a communicable disease is significantly different in one country than in another country. Since the initial data in the Swash-Backwash Model should be balanced, *entity-based bootstrap sampling* is carried out in the `compare_countries()` function. This means that not, for example, 80% of all observations are included in each sample at a sample ratio equal to  $p = 0.8$ , but rather all observations for 80% of the regions. For both countries,  $B$  bootstrap samples (default: 100) are drawn for which the Swash-Backwash Model is calculated. Based on the distribution of indicators, confidence intervals are calculated at the user-specified significance level  $\alpha$ . The `compare_countries()` function calculates the differences of the user's desired indicator between the two samples,  $D$ , and also calculates  $\alpha$  confidence intervals for this.

**Value**

object of class `countries`, see [countries-class](#)

**Author(s)**

Thomas Wieland

## References

*Swash-Backwash Model:*

Cliff AD, Haggett P (2006) A swash-backwash model of the single epidemic wave. *Journal of Geographical Systems* 8(3), 227-252. doi:[10.1007/s1010900600278](https://doi.org/10.1007/s1010900600278)

Smallman-Raynor MR, Cliff AD, Stickler PJ (2022) Meningococcal Meningitis and Coal Mining in Provincial England: Geographical Perspectives on a Major Epidemic, 1929–33. *Geographical Analysis* 54, 197–216. doi:[10.1111/gean.12272](https://doi.org/10.1111/gean.12272)

Smallman-Raynor MR, Cliff AD, The COVID-19 Genomics UK (COG-UK) Consortium (2022) Spatial growth rate of emerging SARS-CoV-2 lineages in England, September 2020–December 2021. *Epidemiology and Infection* 150, e145. doi:[10.1017/S0950268822001285](https://doi.org/10.1017/S0950268822001285).

*Bootstrapping und bootstrap confidence intervals:*

Efron B, Tibshirani RJ (1993) An Introduction to the Bootstrap.

Ramachandran KM, Tsokos CP (2021) Mathematical Statistics with Applications in R (Third Edition). Ch. 13.3.1 (Bootstrap confidence intervals). doi:[10.1016/B9780128178157.000130](https://doi.org/10.1016/B9780128178157.000130)

## See Also

[swash](#), [countries-class](#)

## Examples

```
data(COVID19Cases_geoRegion)
# Get Swiss COVID19 cases at NUTS 3 level

data(Oesterreich_Faelle)
# Get Austrian COVID19 cases at NUTS 3 level
# (first wave, same final date as in Swiss data: 2020-05-31)

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[!COVID19Cases_geoRegion$geoRegion %in% c("CH", "CHFL"),]
# Exclude CH = Switzerland total and CHFL = Switzerland and Liechtenstein total

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[COVID19Cases_geoRegion$datum <= "2020-05-31",]
# Extract first COVID-19 wave

CH_covidwave1 <-
  swash (
    data = COVID19Cases_geoRegion,
    col_cases = "entries",
    col_date = "datum",
    col_region = "geoRegion"
  )
# Swash-Backwash Model for Swiss COVID19 cases
# Spatial aggregate: NUTS 3 (cantons)

AT_covidwave1 <-
  swash (
    data = Oesterreich_Faelle,
```



```

      col_cases = "Faelle",
      col_date = "Datum",
      col_region = "NUTS3"
    )
# Swash-Backwash Model for Austrian COVID19 cases
# Spatial aggregate: NUTS 3

AT_vs_CH <-
  compare_countries(
    CH_covidwave1,
    AT_covidwave1,
    country_names = c("Switzerland", "Austria"))
# Country comparison Switzerland vs. Austria
# default config: 20 iterations, alpha = 0.05, sample ratio = 80%,
# indicator: R_0A

summary(AT_vs_CH)
# Summary of country comparison

plot(AT_vs_CH)
# Plot of country comparison

```

---

 confint-methods

---

*Methods for Function confint*


---

## Description

Methods for function confint

## Methods

`signature(object = "sbm", iterations = 100, samples_ratio = 0.8, alpha = 0.05, replace = TRUE)`

Creates bootstrap confidence intervals for sbm objects. The argument `iterations` indicates the number of bootstrap samples which are drawn. Since the initial data in the Swash-Backwash Model should be balanced, *entity-based bootstrap sampling* is carried out. This means that not, for example, 80% of all observations are included in each sample at a sample ratio equal to  $p = 0.8$  (`samples_ratio = 0.8`), but rather all observations for 80% of the regions. The significance level for the confidence intervals  $\alpha$  is set by the argument `alpha` (default: 0.05, which corresponds to a 95% confidence level).

## Author(s)

Thomas Wieland

## References

*Swash-Backwash Model:*

Cliff AD, Haggett P (2006) A swash-backwash model of the single epidemic wave. *Journal of Geographical Systems* 8(3), 227-252. doi:[10.1007/s1010900600278](https://doi.org/10.1007/s1010900600278)

Smallman-Raynor MR, Cliff AD, Stickler PJ (2022) Meningococcal Meningitis and Coal Mining in Provincial England: Geographical Perspectives on a Major Epidemic, 1929–33. *Geographical Analysis* 54, 197–216. doi:10.1111/gean.12272

Smallman-Raynor MR, Cliff AD, The COVID-19 Genomics UK (COG-UK) Consortium (2022) Spatial growth rate of emerging SARS-CoV-2 lineages in England, September 2020–December 2021. *Epidemiology and Infection* 150, e145. doi:10.1017/S0950268822001285.

*Bootstrapping und bootstrap confidence intervals:*

Efron B, Tibshirani RJ (1993) An Introduction to the Bootstrap.

Ramachandran KM, Tsokos CP (2021) Mathematical Statistics with Applications in R (Third Edition). Ch. 13.3.1 (Bootstrap confidence intervals). doi:10.1016/B9780128178157.000130

## See Also

[sbm\\_ci-class](#)

---

countries-class	Class "countries"
-----------------	-------------------

---

## Description

The class "countries" contains the results of a two-country comparison analysis using the Swash-Backwash Model, including two "sbm\_ci" classes for each country. Use `summary(countries)` and `plot(countries)` for results summary and plotting, respectively.

## Objects from the Class

Objects can be created by calls of the form `new("countries", ...)`. Objects can be created by the function `compare_countries(sbm1, sbm2)`.

## Slots

`sbm_ci1`: Object of class "sbm\_ci" Results of `confint(sbm1)` for country 1

`sbm_ci2`: Object of class "sbm\_ci" Results of `confint(sbm1)` for country 2

`D`: Object of class "numeric" Results: Difference  $D$  between the samples with respect to the chosen indicator

`D_ci`: Object of class "numeric" Results:  $\alpha$  confidence intervals of  $D$

`config`: Object of class "list" Configuration details for bootstrap sampling

`country_names`: Object of class "character" User-stated country names

`indicator`: Object of class "character" User-stated indicator to be tested

**Methods**

**plot** signature(x = "countries"): Plots the results of a two-country comparison with the Swash-Backwash Model

**show** signature(object = "countries"): Prints an countries object; use summary(sbm\_ci) for results

**summary** signature(object = "countries"): Prints a summary of a countries object (results of the two-country comparison)

**Author(s)**

Thomas Wieland

**Examples**

```
showClass("countries")
```

---

COVID19Cases\_geoRegion

*Switzerland Daily COVID-19 cases by region*

---

**Description**

A dataset containing COVID-19 cases by region (NUTS 3 = cantons) and time periods (days) for Switzerland (Source: Federal Office of Public Health FOPH).

**Usage**

```
data(COVID19Cases_geoRegion)
```

**Format**

A data.frame with multiple columns:

**geoRegion** (character) Region for which the data was collected.

**datum** (Date) Date of record.

**entries** (integer) Number of reported cases on this date.

**sumTotal** (integer) Cumulative case numbers.

**timeframe\_14d** (logical) Indicates whether the time period covers the last 14 days.

**timeframe\_all** (logical) Indicates whether the time period covers all previous data.

**offset\_last7d** (integer) Offset of the last 7 days.

**sumTotal\_last7d** (integer) Cumulative case numbers of the last 7 days.

**offset\_last14d** (integer) Offset of the last 14 days.

**sumTotal\_last14d** (integer) Cumulative case numbers of the last 14 days.

**offset\_last28d** (integer) Offset of the last 28 days.

**sumTotal\_last28d** (integer) Cumulative case numbers of the last 28 days.

**sum7d** (numeric) Sum of the last 7 days.

**sum14d** (numeric) Sum of the last 14 days.

**mean7d** (numeric) Average of the last 7 days.

**mean14d** (numeric) Average of the last 14 days.

**entries\_diff\_last\_age** (integer) Difference from the last age group.

**pop** (integer) Population of the region.

**inz\_entries** (numeric) Incidence of the entries.

**inzsumTotal** (numeric) Incidence of cumulative cases.

**inzmean7d** (numeric) Incidence of the 7-day average.

**inzmean14d** (numeric) Incidence of the 14-day average.

**inzsumTotal\_last7d** (numeric) Incidence of cumulative cases in the last 7 days.

**inzsumTotal\_last14d** (numeric) Incidence of cumulative cases in the last 14 days.

**inzsumTotal\_last28d** (numeric) Incidence of cumulative cases in the last 28 days.

**inzsum7d** (numeric) Incidence of the last 7 days.

**inzsum14d** (numeric) Incidence of the last 14 days.

**sumdelta7d** (numeric) Difference in sums of the last 7 days.

**inzdelta7d** (numeric) Difference in incidence of the last 7 days.

**type** (character) Type of recorded data (e.g., COVID-19 cases).

**type\_variant** (character) Variant of the data type.

**version** (character) Version of the data collection.

**datum\_unit** (character) Unit of date specification (e.g., day).

**entries\_letzter\_stand** (integer) Last known count of entries.

**entries\_neu\_gemeldet** (integer) Newly reported entries.

**entries\_diff\_last** (integer) Difference in last entries.

## Details

The data is included as it was published in by the Swiss Federal Office of Public Health (Bundesamt fuer Gesundheit, BAG). Note that the reporting date equals the date of SARS-CoV-2 testing.

## Source

Federal Office of Public Health FOPH (2023) COVID-19 Dashboard Source Data. <https://www.covid19.admin.ch/api/data/documentation> (retrieved 2023-06-28)

**Examples**

```

data(COVID19Cases_geoRegion)
# Get SWISS COVID19 cases at NUTS 3 level

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[!COVID19Cases_geoRegion$geoRegion %in% c("CH", "CHFL"),]
# Exclude CH = Switzerland total and CHFL = Switzerland and Liechtenstein total

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[COVID19Cases_geoRegion$datum <= "2020-05-31",]
# Extract first COVID-19 wave

COVID19Cases_geoRegion_balanced <-
  is_balanced(
    data = COVID19Cases_geoRegion,
    col_cases = "entries",
    col_date = "datum",
    col_region = "geoRegion"
  )
# Test whether "COVID19Cases_geoRegion" is balanced panel data

COVID19Cases_geoRegion_balanced$data_balanced
# Balanced? TRUE or FALSE

```

---

exponential_growth	<i>Exponential Growth Model for Epidemic Data</i>
--------------------	---

---

**Description**

Estimation of exponential growth models from daily infections data

**Usage**

```

exponential_growth(
  y,
  t,
  GI = 4
)

```

**Arguments**

y	numeric vector with cumulative infections data over time
t	vector of class numeric or Date with time points or dates
GI	Generation interval for computing $R_0$

## Details

This function allows the estimation of an exponential growth model. The user must specify the dependent variable (daily infections) and the time variable (time counter or date values). The estimation is performed using a linearized model as an OLS estimator. The results are the exponential growth rate  $r$ , basic reproduction number  $R_0$ , and the doubling rate.

## Value

list with four entries:

exp_gr:	numeric value of exponential growth rate
$R_0$ :	numeric value of basic reproduction number
doubling:	numeric value of doubling rate
model_data:	lm object of regression model

## Author(s)

Thomas Wieland

## References

Bonifazi G et al. (2021) A simplified estimate of the effective reproduction number  $R_t$  using its relation with the doubling time and application to Italian COVID-19 data. *The European Physical Journal Plus* 136, 386. doi:[10.1140/epjp/s13360021013396](https://doi.org/10.1140/epjp/s13360021013396)

Chowell G, Viboud C, Hyman JM, Simonsen L (2015) The Western Africa ebola virus disease epidemic exhibits both global exponential and local polynomial growth rates. *PLOS Currents Outbreaks*, ecurrents.outbreaks.8b55f4bad99ac5c5db3663e916803261. doi:[10.1371/currents.outbreaks.8b55f4bad99ac5c5db3663e916803261](https://doi.org/10.1371/currents.outbreaks.8b55f4bad99ac5c5db3663e916803261)

Pell B, Kuang Y, Viboud C, Chowell G (2018) Using phenomenological models for forecasting the 2015 ebola challenge. *Epidemics* 22, 62–70. doi:[10.1016/j.epidem.2016.11.002](https://doi.org/10.1016/j.epidem.2016.11.002)

Wieland T (2020) A phenomenological approach to assessing the effectiveness of COVID-19 related nonpharmaceutical interventions in Germany. *Safety Science* 131, 104924. doi:[10.1016/j.ssci.2020.104924](https://doi.org/10.1016/j.ssci.2020.104924)

## See Also

[growth\\_initial](#), [logistic\\_growth](#)

## Examples

```
data(COVID19Cases_geoRegion)
# Get SWISS COVID19 cases at NUTS 3 level

COVID19Cases_ZH <-
  COVID19Cases_geoRegion[(COVID19Cases_geoRegion$geoRegion == "ZH")
    & (COVID19Cases_geoRegion$sumTotal > 0),]
# COVID cases for Zurich

expgrowth_BS <- exponential_growth (
```

```

    y = COVID19Cases_ZH$sumTotal[1:28],
    t = COVID19Cases_ZH$datum[1:28]
  )
  # Exponential growth model for the first 4 weeks

  expgrowth_BS$doubling
  # Doubling rate

```

---

growth

---

*Logistic Growth Models for Regional Infections*


---

## Description

Estimates  $N$  logistic growth models for  $N$  regions.

## Usage

```

growth(
  object,
  S_iterations = 10,
  S_start_est_method = "bisect",
  seq_by = 10,
  nls = TRUE
)

```

## Arguments

object	object of class sbm
S_iterations	Number of iterations for saturation value search
S_start_est_method	Method for saturation value search, either "bisect" or "trial_and_error"
seq_by	No of segments for the "trial_and_error" estimation of the saturation value
nls	Nonlinear estimation? TRUE or FALSE

## Details

The function estimates logistic growth models for regional infections based on a sbm object. See [logistic\\_growth](#) for further details.

## Value

list with two entries:

results:	Object of class "data.frame" Results of the logistic growth models (coefficients and derivatives)
logistic_growth_models:	Object of class "list" List with $N$ entries for $N$ growth models resp. loggrowth objects

**Author(s)**

Thomas Wieland

**References**

Chowell G, Simonsen L, Viboud C, Yang K (2014) Is West Africa Approaching a Catastrophic Phase or is the 2014 Ebola Epidemic Slowing Down? Different Models Yield Different Answers for Liberia. *PLoS currents* 6. doi:[10.1371/currents.outbreaks.b4690859d91684da963dc40e00f3da81](https://doi.org/10.1371/currents.outbreaks.b4690859d91684da963dc40e00f3da81)

Pell B, Kuang Y, Viboud C, Chowell G (2018) Using phenomenological models for forecasting the 2015 ebola challenge. *Epidemics* 22, 62–70. doi:[10.1016/j.epidem.2016.11.002](https://doi.org/10.1016/j.epidem.2016.11.002)

Wieland T (2020) Flatten the Curve! Modeling SARS-CoV-2/COVID-19 Growth in Germany at the County Level. *REGION* 7(2), 43–83. doi:[10.18335/region.v7i2.324](https://doi.org/10.18335/region.v7i2.324)

**See Also**

[logistic\\_growth](#), [exponential\\_growth](#)

**Examples**

```
data(COVID19Cases_geoRegion)
# Get SWISS COVID19 cases at NUTS 3 level

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[!COVID19Cases_geoRegion$geoRegion %in% c("CH", "CHFL"),]
# Exclude CH = Switzerland total and CHFL = Switzerland and Liechtenstein total

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[COVID19Cases_geoRegion$datum <= "2020-05-31",]
# Extract first COVID-19 wave

CH_covidwave1 <-
  swash (
    data = COVID19Cases_geoRegion,
    col_cases = "entries",
    col_date = "datum",
    col_region = "geoRegion"
  )
# Swash-Backwash Model for Swiss COVID19 cases
# Spatial aggregate: NUTS 3 (cantons)

CH_covidwave1_growth <- growth(CH_covidwave1)
CH_covidwave1_growth
# Logistic growth models for sbm object CH_covidwave1
```



---

growth-methods	<i>Methods for Function growth</i>
----------------	------------------------------------

---

**Description**

Methods for function growth

**Methods**

```
signature(object = "sbm", S_iterations = 10, S_start_est_method = "bisect", seq_by = 10, nls = TRUE)
```

Estimation of  $N$  logistic growth models for  $N$  regions. Both OLS and NLS estimation are estimated by default (set `nls = FALSE` to skip NLS estimation). Parameters `S_iterations`, `S_start_est_method`, and `seq_by` are used to control the saturation value estimation (see [logistic\\_growth](#)).

**Author(s)**

Thomas Wieland

---

growth_initial	<i>Exponential Growth Models for Regional Infections</i>
----------------	--

---

**Description**

Estimates  $N$  exponential growth models for a given time period in  $N$  regions.

**Usage**

```
growth_initial(
  object,
  time_units = 10,
  GI = 4
)
```

**Arguments**

<code>object</code>	object of class <code>sbm</code>
<code>time_units</code>	numeric value for the analysis time (time units from start)
<code>GI</code>	Generation interval for computing $R_0$

**Details**

The function estimates exponential growth models for regional infections based on a `sbm` object. Such models are design for the analysis of the *initial* phase of an epidemic spread. The user must state how much time units (from start) are included. See [exponential\\_growth](#) for further details of the estimation.

**Value**

list with two entries:

results: Object of class "data.frame" Results of the exponential growth models (growth rate, basic reproduction number, doubling rate) for each region

exponential\_growth\_models: Object of class "list" List with  $N$  entries for  $N$  exponential models

**Author(s)**

Thomas Wieland

**References**

Bonifazi G et al. (2021) A simplified estimate of the effective reproduction number  $R_t$  using its relation with the doubling time and application to Italian COVID-19 data. *The European Physical Journal Plus* 136, 386. doi:10.1140/epjp/s13360021013396

Chowell G, Viboud C, Hyman JM, Simonsen L (2015) The Western Africa ebola virus disease epidemic exhibits both global exponential and local polynomial growth rates. *PLOS Currents Outbreaks*, ecurrents.outbreaks.8b55f4bad99ac5c5db3663e916803261. doi:10.1371/currents.outbreaks.8b55f4bad99ac5c5db36

Pell B, Kuang Y, Viboud C, Chowell G (2018) Using phenomenological models for forecasting the 2015 ebola challenge. *Epidemics* 22, 62–70. doi:10.1016/j.epidem.2016.11.002

Wieland T (2020) A phenomenological approach to assessing the effectiveness of COVID-19 related nonpharmaceutical interventions in Germany. *Safety Science* 131, 104924. doi:10.1016/j.ssci.2020.104924

**Examples**

```
data(COVID19Cases_geoRegion)
# Get SWISS COVID19 cases at NUTS 3 level

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[!COVID19Cases_geoRegion$geoRegion %in% c("CH", "CHFL"),]
# Exclude CH = Switzerland total and CHFL = Switzerland and Liechtenstein total

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[COVID19Cases_geoRegion$datum <= "2020-05-31",]
# Extract first COVID-19 wave

CH_covidwave1 <-
  swash (
    data = COVID19Cases_geoRegion,
    col_cases = "entries",
    col_date = "datum",
    col_region = "geoRegion"
  )
# Swash-Backwash Model for Swiss COVID19 cases
# Spatial aggregate: NUTS 3 (cantons)

CH_covidwave1_initialgrowth_3weeks <-
```

```

growth_initial(
  CH_covidwave1,
  time_units = 21
)
CH_covidwave1_initialgrowth_3weeks$results
# Exponential models for sbm object CH_covidwave1
# initial growth in the first 3 weeks

```

---

growth\_initial-methods

*Methods for Function growth\_initial*

---

## Description

Methods for function growth\_initial

## Methods

signature(object = "sbm", time\_units = 10, GI = 4) Estimation of  $N$  exponential growth models for the initial phase of an epidemic spread for  $N$  regions. Set argument GI for the calculation of the basic reproduction number(see [exponential\\_growth](#)).

## Author(s)

Thomas Wieland

---

hist\_ci

*Creating Histograms with Confidence Intervals*

---

## Description

Plot of a histogram of a given vector x and the related confidence intervals (lower, upper).

## Usage

```

hist_ci(
  x,
  alpha = 0.05,
  colBars = "grey",
  col_ci = "red",
  ...
)

```

**Arguments**

x	A numeric vector
alpha	Significance level $\alpha$ for $1-\alpha*100$ confidence intervals
col_bars	Color of bars in histogram
col_ci	Color of lines for confidence interval
...	Additional arguments passed to <code>barplot()</code>

**Details**

Helper function for `plot(sbm_ci)`, but may be used separately.

**Value**

Histogram plot, no returned value

**Author(s)**

Thomas Wieland

**Examples**

```
numeric_vector <- c(1,9,5,6,3,10,20,6,9,14,3,5,8,6,11)
# any numeric vector

hist_ci(numeric_vector)
```

---

is\_balanced

---

*Test whether Panel Dataset with Regional Infection Data is Balanced*


---

**Description**

The function tests whether the input panel data with regional infections is balanced.

**Usage**

```
is_balanced(
  data,
  col_cases,
  col_date,
  col_region,
  as_balanced = TRUE,
  fill_missing = 0
)
```

**Arguments**

data	data.frame with regional infection data
col_cases	Column containing the cases (numeric)
col_date	Column containing the time points (e.g., days)
col_region	Column containing the unique identifier of the regions (e.g., name, NUTS 3 code)
as_balanced	Boolean argument which indicates whether non-balanced panel data shall be balanced (default: TRUE)
fill_missing	Constant to fill missing values (default and recommended: 0)

**Details**

The Swash-Backwash Model for the Single Epidemic Wave does not necessarily require balanced panel data in order for the calculations to be carried out. However, for a correct estimation it is implicitly assumed that the input data is balanced. The function tests whether the panel data is balanced. It is executed automatically within the `swash()` function (using automatic correction with `as_balanced = TRUE`), but can also be used separately.

**Value**

List with two entries:

data_balanced	Result of test (TRUE or FALSE)
data	Input dataset (data.frame)

**Author(s)**

Thomas Wieland

**References**

*Swash-Backwash Model:*

Cliff AD, Haggett P (2006) A swash-backwash model of the single epidemic wave. *Journal of Geographical Systems* 8(3), 227-252. doi:[10.1007/s1010900600278](https://doi.org/10.1007/s1010900600278)

Smallman-Raynor MR, Cliff AD, Stickler PJ (2022) Meningococcal Meningitis and Coal Mining in Provincial England: Geographical Perspectives on a Major Epidemic, 1929–33. *Geographical Analysis* 54, 197–216. doi:[10.1111/gean.12272](https://doi.org/10.1111/gean.12272)

Smallman-Raynor MR, Cliff AD, The COVID-19 Genomics UK (COG-UK) Consortium (2022) Spatial growth rate of emerging SARS-CoV-2 lineages in England, September 2020–December 2021. *Epidemiology and Infection* 150, e145. doi:[10.1017/S0950268822001285](https://doi.org/10.1017/S0950268822001285).

*Panel data:*

Greene, WH (2012) *Econometric Analysis*. Ch. 11.

Wooldridge, JM (2012) *Introductory Econometrics. A Modern Approach*. Ch. 13.

**See Also**[as\\_balanced](#)**Examples**

```

data(COVID19Cases_geoRegion)
# Get SWISS COVID19 cases at NUTS 3 level

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[!COVID19Cases_geoRegion$geoRegion %in% c("CH", "CHFL"),]
# Exclude CH = Switzerland total and CHFL = Switzerland and Liechtenstein total

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[COVID19Cases_geoRegion$datum <= "2020-05-31",]
# Extract first COVID-19 wave

COVID19Cases_geoRegion_balanced <-
  is_balanced(
    data = COVID19Cases_geoRegion,
    col_cases = "entries",
    col_date = "datum",
    col_region = "geoRegion"
  )
# Test whether "COVID19Cases_geoRegion" is balanced panel data

COVID19Cases_geoRegion_balanced$data_balanced
# Balanced? TRUE or FALSE

if (COVID19Cases_geoRegion_balanced$data_balanced == FALSE) {
  COVID19Cases_geoRegion <-
    as_balanced(
      COVID19Cases_geoRegion,
      col_cases = "entries",
      col_date = "datum",
      col_region = "geoRegion"
    )
}
# Correction of dataset "COVID19Cases_geoRegion"
# not necessary as parameter balance of is_balanced is set TRUE by default

```

loggrowth-class

*Class "loggrowth"***Description**

The class "loggrowth" contains the results of the `logistic_growth()` function. Use `summary(sbm)` and `plot(sbm)` for results summary and plotting, respectively.

## Objects from the Class

Objects can be created by the function `logistic_growth`.

## Slots

**LinModel:** Object of class `list` Results of the OLS helper model

**GrowthModel\_OLS:** Object of class `list` Results of the OLS fit (predicted, parameters, first derivative)

**GrowthModel\_NLS:** Object of class `list` Results of the NLS fit (predicted, parameters, first derivative)

**t:** Object of class `numeric` Input time points data

**y:** Object of class `numeric` Input infections data

**config:** Object of class `list` Model fit configurations

## Methods

**plot** signature(`x` = "loggrowth"): Plots the results of the logistic growth model (observed, predicted, first derivative)

**summary** signature(`object` = "loggrowth"): Prints a summary of loggrowth objects

## Author(s)

Thomas Wieland

## References

Wieland T (2020) Flatten the Curve! Modeling SARS-CoV-2/COVID-19 Growth in Germany at the County Level. *REGION* 7(2), 43–83. doi:[10.18335/region.v7i2.324](https://doi.org/10.18335/region.v7i2.324)

## Examples

```
showClass("loggrowth")
```

---

logistic\_growth

---

*Logistic Growth Model for Epidemic Data*


---

## Description

Estimation of logistic growth models from cumulative infections data, linearized OLS and/or NLS

**Usage**

```
logistic_growth(  
  y,  
  t,  
  S = NULL,  
  S_start = NULL,  
  S_end = NULL,  
  S_iterations = 10,  
  S_start_est_method = "bisect",  
  seq_by = 10,  
  nls = TRUE  
)
```

**Arguments**

y	numeric vector with cumulative infections data over time
t	vector of class numeric or Date with time points or dates
S	Saturation value for the model
S_start	Start value of the saturation value for estimation
S_end	End value of the saturation value for estimation
S_iterations	Number of iterations for saturation value search
S_start_est_method	Method for saturation value search, either "bisect" or "trial_and_error"
seq_by	No of segments for the "trial_and_error" estimation of the saturation value
nls	Nonlinear estimation? TRUE or FALSE

**Details**

This function allows the estimation of a logistic growth model. The user must specify the dependent variable (cumulative infections) and the time variable (time counter or date values). The estimation is performed using a linearized model as an OLS estimator and as an NLS estimator. For the former, the saturation value can either be specified by the user or found using a search algorithm. The parameters from the OLS fit are used as starting values for the NLS estimation.

**Value**

object of class `loggrowth-class`

**Author(s)**

Thomas Wieland



## References

- Chowell G, Simonsen L, Viboud C, Yang K (2014) Is West Africa Approaching a Catastrophic Phase or is the 2014 Ebola Epidemic Slowing Down? Different Models Yield Different Answers for Liberia. *PLoS currents* 6. doi:[10.1371/currents.outbreaks.b4690859d91684da963dc40e00f3da81](https://doi.org/10.1371/currents.outbreaks.b4690859d91684da963dc40e00f3da81)
- Pell B, Kuang Y, Viboud C, Chowell G (2018) Using phenomenological models for forecasting the 2015 ebola challenge. *Epidemics* 22, 62–70. doi:[10.1016/j.epidem.2016.11.002](https://doi.org/10.1016/j.epidem.2016.11.002)
- Wieland T (2020) Flatten the Curve! Modeling SARS-CoV-2/COVID-19 Growth in Germany at the County Level. *REGION* 7(2), 43–83. doi:[10.18335/region.v7i2.324](https://doi.org/10.18335/region.v7i2.324)

## See Also

[loggrowth-class](#), [growth](#), [exponential\\_growth](#)

## Examples

```
data(COVID19Cases_geoRegion)
# Get SWISS COVID19 cases at NUTS 3 level

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[!COVID19Cases_geoRegion$geoRegion %in% c("CH", "CHFL"),]
# Exclude CH = Switzerland total and CHFL = Switzerland and Liechtenstein total

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[COVID19Cases_geoRegion$datum <= "2020-05-31",]
# Extract first COVID-19 wave

COVID19Cases_BS <-
  COVID19Cases_geoRegion[(COVID19Cases_geoRegion$geoRegion == "ZH")
    & (COVID19Cases_geoRegion$sumTotal > 0),]
# COVID cases for Zurich

loggrowth_BS <- logistic_growth (
  y = as.numeric(COVID19Cases_BS$sumTotal),
  t = COVID19Cases_BS$datum,
  S = 5557,
  S_start = NULL,
  S_end = NULL,
  S_iterations = 10,
  S_start_est_method = "bisect",
  seq_by = 10,
  nls = TRUE
)
# Logistic growth model with stated saturation value

summary(loggrowth_BS)
# Summary of logistic growth model

plot(loggrowth_BS)
# Plot of logistic growth model
```

nbmatrix

*Construct Neighbourhood Matrix from Polygons***Description**

Building a neighbourhood matrix based on regions (polygons) with contiguous boundaries and resulting a data frame

**Usage**

```
nbmatrix(
  polygon_sf,
  ID_col,
  row.names = NULL
)
```

**Arguments**

polygon_sf	sf object with polygons
ID_col	Column of polygon_sf with unique ID of each polygon
row.names	row.names for the sf object

**Details**

The function is based on `spdep::poly2nb`, which creates neighbours lists. The input is a `sf` object (spatial data frame) and the results are 1) a `nb` list (`poly2nb` result) and 2) a `data.frame`.

**Value**

list with two entries:

nb:	Object of class "nb" Neighbours list; see the <code>spdep::poly2nb</code> documentation
nbmat:	Object of class "data.frame" Dataset neighbouring regions

**Author(s)**

Thomas Wieland

**References**

Wieland T (2020) Flatten the Curve! Modeling SARS-CoV-2/COVID-19 Growth in Germany at the County Level. *REGION* 7(2), 43–83. doi:[10.18335/region.v7i2.324](https://doi.org/10.18335/region.v7i2.324)

Wieland T (2022) Spatial patterns of excess mortality in the first year of the COVID-19 pandemic in Germany. *European Journal of Geography* 13(4), 18-33. doi:[10.48088/ejg.t.wie.13.4.018.033](https://doi.org/10.48088/ejg.t.wie.13.4.018.033)

**See Also**

[nbstat](#)

## Examples

```
data(RKI_Corona_counties)
# German counties (Source: Robert Koch Institute)

Corona_nbmat <-
  nbmatrix (
    RKI_Corona_counties,
    ID_col="AGS"
  )
# Creating neighborhood matrix
```

---

nbstat

---

*Calculate Neighbourhood Statistics from Polygons*


---

## Description

Calculating descriptive neighbourhood statistics based on regions (polygons) with contiguous boundaries and resulting a data frame

## Usage

```
nbstat(
  polygon_sf,
  ID_col,
  link_data,
  data_ID_col,
  data_col,
  func = "sum",
  row.names = NULL
)
```

## Arguments

<code>polygon_sf</code>	sf object with polygons
<code>ID_col</code>	Column of <code>polygon_sf</code> with unique ID of each polygon
<code>link_data</code>	<code>data.frame</code> to merge with
<code>data_ID_col</code>	Column with unique ID of each polygon in <code>data.frame</code>
<code>data_col</code>	Column with regarded numeric values in <code>data.frame</code>
<code>func</code>	Descriptive statistic (FUN) to be computed for <code>data_col</code> of the neighbouring regions
<code>row.names</code>	<code>row.names</code> for the sf object

## Details

The function is based on `spdep::poly2nb`, which creates neighbours lists. The input is a `sf` object (spatial data frame) and the results are 1) a `nb` list (`poly2nb` result) and 2) a `data.frame`.

**Value**

list with three entries:

nbmat: Object of class "data.frame" Dataset neighbouring regions  
 nbmat\_data: Object of class "data.frame" Dataset neighbouring regions and linked data  
 nbmat\_data\_aggreagte: Object of class "data.frame" Dataset with statistic by region

**Author(s)**

Thomas Wieland

**References**

Wieland T (2020) Flatten the Curve! Modeling SARS-CoV-2/COVID-19 Growth in Germany at the County Level. *REGION* 7(2), 43–83. doi:[10.18335/region.v7i2.324](https://doi.org/10.18335/region.v7i2.324)

Wieland T (2022) Spatial patterns of excess mortality in the first year of the COVID-19 pandemic in Germany. *European Journal of Geography* 13(4), 18-33. doi:[10.48088/ejg.t.wie.13.4.018.033](https://doi.org/10.48088/ejg.t.wie.13.4.018.033)

**See Also**

[nbmatrix](#)

**Examples**

```
data(RKI_Corona_counties)
# German counties (Source: Robert Koch Institute)

Corona_nbstat <-
  nbstat (
    RKI_Corona_counties,
    ID_col="AGS",
    link_data = RKI_Corona_counties,
    data_ID_col = "AGS",
    data_col = "EWZ",
    func = "sum"
  )
Corona_nbstat$nbmat_data_aggregate
# Sum of population (EWZ) of neighbouring counties
```

---

Oesterreich\_Faelle      *Austria Daily COVID-19 cases by region 2020-02-26 to 2020-05-31*

---

**Description**

A dataset containing COVID-19 cases by region (NUTS 3) and time periods (days) for Austria (Source: BMSGPK).

**Usage**

```
data(Oesterreich_Faelle)
```

**Format**

A data.frame with multiple columns:

**NUTS3** (character) Region for which the data was collected.

**Datum** (Date) Date of record.

**Faelle** (integer) Number of reported cases on this date.

**Details**

The original data was originally published by BMSGPK at a smaller spatial scale level (political districts, "Politische Bezirke"). The data was linked to a corresponding shapefile from Statistik Austria (2022), joined to the NUTS3 level via a spatial join, and summed over the Austrian NUTS3 regions. The spatial join is based on polygon centroids of the political districts level; in cases where the centroid was outside the polygon, it was placed inside the polygon manually.

**Source**

BMSGPK, Oesterreichisches COVID-19 Open Data Informationsportal (2022) COVID-19: Zeitliche Darstellung von Daten zu Covid19-Faellen je Bezirk. <https://www.data.gv.at/katalog/dataset/4b71eb3d-7d55-4967-b80d-91a3f220b60c> (retrieved 2022-06-23)

Statistik Austria (2022) Politische Bezirke. [https://www.data.gv.at/katalog/dataset/stat\\_gliederung-osterreichs-in-politische-bezirke131e2](https://www.data.gv.at/katalog/dataset/stat_gliederung-osterreichs-in-politische-bezirke131e2) (retrieved 2022-06-27)

Wieland T (2022) C19dNUTS: Dataset of Regional COVID-19 Deaths per 100,000 Pop (NUTS). R package v1.0.1. [doi:10.32614/CRAN.package.C19dNUTS](https://doi.org/10.32614/CRAN.package.C19dNUTS)

**Examples**

```
data(Oesterreich_Faelle)
# Get Austrian COVID19 cases at NUTS 3 level
# (first wave, same final date as in Swiss data: 2020-05-31)

AT_covidwave1 <-
  swash (
    data = Oesterreich_Faelle,
    col_cases = "Faelle",
    col_date = "Datum",
    col_region = "NUTS3"
  )
# Swash-Backwash Model for Austrian COVID19 cases
# Spatial aggregate: NUTS 3

summary(AT_covidwave1)
# Summary of model results
```

## Description

Methods for function plot for different S4 classes: `sbm`, `sbm_ci`, and `loggrowth`.

## Methods

`signature(x = "sbm") plot.sbm(x, y, ...)`: Plots the results of the Swash-Backwash Model.

This generates two plots:

- Edges over time.
- Total infections per time unit.

### Arguments:

- `x`: An object of class `sbm` representing the results of the Swash-Backwash Model.
- `y`: Optional argument for additional customization, such as plot style or axis labels.
- `...`: Additional graphical parameters that can be passed to control plot appearance.

**Details:** This method is used to visualize the output of the Swash-Backwash Model, providing insight into the dynamics of the modeled epidemic.

`signature(x = "sbm_ci") plot.sbm_ci(x, y, ...)`: Plots the results of bootstrap confidence intervals for the Swash-Backwash Model. This generates a single figure with six subplots:

- $S_A$  (susceptible population),
- $I_A$  (infected population),
- $R_A$  (recovered population),
- $t_{FE}$  (final epidemic time),
- $t_{LE}$  (last epidemic time),
- $R_{0A}$  (basic reproduction number).

### Arguments:

- `x`: An object of class `sbm_ci` containing the bootstrap confidence intervals for the Swash-Backwash Model.
- `y`: Optional argument for additional customization, such as plot style or axis labels.
- `...`: Additional graphical parameters for fine-tuning the plots.

**Details:** This method is used to visualize the bootstrap confidence intervals for various parameters of the Swash-Backwash Model.

`signature(x = "countries") plot.sbm(x, y = NULL, colBars = "grey", col_ci = "red")`: Plots the results of the between-countries analysis via Swash-Backwash Model. This generates four plots:

- Indicator for country 1
- Indicator for country 2
- Boxplots of the distribution of the indicator in country 1 and 2
- Distribution of the difference between the indicators of country 1 and 2

**Arguments:**

- `x`: An object of class `countries` representing the results of the Swash-Backwash Model country analysis.
- `y`: Not relevant
- `col_bars`: Color of bars
- `col_ci`: Color of confidence intervals

**Details:** This method is used to visualize the output of the Swash-Backwash Model, providing insight into the dynamics of the modeled epidemic.

`signature(x = "loggrowth") plot.loggrowth(x, y, ...)`: Plots the results of the logistic growth model, including:

- Observed values,
- Predicted values,
- First derivative (growth rate).

**Arguments:**

- `x`: An object of class `loggrowth` containing the data for the logistic growth model.
- `y`: Optional argument for additional customization of the plot (e.g., color, labels).
- `...`: Additional arguments for graphical parameters.

**Details:** This method is useful for visualizing the observed and predicted growth patterns in an epidemic or similar phenomena modeled by logistic growth.

**Author(s)**

Thomas Wieland

---

plot\_regions

*Plots of Regional Infections Over Time*

---

**Description**

Plots regional infection curves in  $N$  plots for  $N$  regions.

**Usage**

```
plot_regions(
  object,
  col = "red",
  scale = FALSE,
  normalize_by_col = NULL,
  normalize_factor = 1
)
```

**Arguments**

object	object of class sbm
col	Color of line plot
scale	Set y axis of the plots uniformly based on the maximum value across all regions? (boolean, default: FALSE)
normalize_by_col	Normalize infection numbers by stating a column in the input data frame (e.g., regional population)
normalize_factor	Multiply density/incidence with a factor (say, 100,000 inhabitants)

**Details**

Plots regional infection curves in  $N$  plots for  $N$  regions, with the number of columns equals 4 and the number of rows is calculated based the size of  $N$ .

**Value**

Plot, only no returned value

**Author(s)**

Thomas Wieland

**Examples**

```
data(COVID19Cases_geoRegion)
# Get SWISS COVID19 cases at NUTS 3 level

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[!COVID19Cases_geoRegion$geoRegion %in% c("CH", "CHFL"),]
# Exclude CH = Switzerland total and CHFL = Switzerland and Liechtenstein total

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[COVID19Cases_geoRegion$datum <= "2020-05-31",]
# Extract first COVID-19 wave

CH_covidwave1 <-
  swash (
    data = COVID19Cases_geoRegion,
    col_cases = "entries",
    col_date = "datum",
    col_region = "geoRegion"
  )
# Swash-Backwash Model for Swiss COVID19 cases
# Spatial aggregate: NUTS 3 (cantons)

plot_regions(CH_covidwave1)
# Plot of regional infections
```



---

plot\_regions-methods    *Methods for Function plot\_regions*

---

## Description

Methods for function plot\_regions

## Methods

signature(object = "sbm", col = "red", scale = FALSE, normalize\_by\_col = NULL, normalize\_factor = 1)

Plots regional infection curves in  $N$  plots for  $N$  regions, with the number of columns equals 4 and the number of rows is calculated based the size of  $N$ . Set the color by the argument col. If scale is TRUE, the y axis of the plots is set uniformly based on the maximum value across all regions. If the input data contains a column to normalize the infection numbers (such as regional population), the user may use this data to normalize the infection numbers by setting normalize\_by\_col. If this density value should be multiplied by a factor (e.g. regional infections per 100,000 inhabitants), this can be set with the argument normalize\_by\_col (default: 1).

## Author(s)

Thomas Wieland

---

print-methods    *Methods for Function print*

---

## Description

Methods for function print

## Methods

signature(x = "sbm") Prints an sbm object; use summary(sbm) for results

signature(x = "sbm\_ci") Prints an sbm\_ci object; use summary(sbm\_ci) for results

---

`quantile_ci`*Computing Quantiles for a given Numeric Vector*

---

**Description**

Computes quantiles for a given vector `x` and the related confidence intervals (lower, upper).

**Usage**

```
quantile_ci(  
  x,  
  alpha = 0.05  
)
```

**Arguments**

<code>x</code>	A numeric vector
<code>alpha</code>	Significance level $\alpha$ for $1-\alpha*100$ confidence intervals

**Details**

Helper function for `plot(sbm_ci)`, but may be used separately.

**Value**

A numeric vector with lower and upper quantile

**Author(s)**

Thomas Wieland

**Examples**

```
numeric_vector <- c(1,9,5,6,3,10,20,6,9,14,3,5,8,6,11)  
# any numeric vector  
  
quantile_ci(numeric_vector)
```

---

RKI\_Corona\_counties     *German Counties with COVID-19 Cases*


---

### Description

A dataset containing German counties (NUTS 3) with COVID-19 cases (Source: Robert Koch Institute).

### Usage

```
data(RKI_Corona_counties)
```

### Format

A data.frame with multiple columns:

**OBJECTID** unknown/not necessary  
**ADE** (unknown/not necessary  
**GF** unknown/not necessary  
**BSG** unknown/not necessary  
**RS** (character) County code 1  
**AGS** (character) County code 2  
**SDV\_RS** (character) County code 3  
**GEN** (character) County name  
**BEZ** (character) County type  
**IBZ** unknown/not necessary  
**BEM** unknown/not necessary  
**NBD** unknown/not necessary  
**SN\_L** unknown/not necessary  
**SN\_R** unknown/not necessary  
**SN\_K** unknown/not necessary  
**SN\_V1** unknown/not necessary  
**SN\_V2** unknown/not necessary  
**SN\_G** unknown/not necessary  
**FK\_S3** unknown/not necessary  
**NUTS** (character) NUTS 3 code  
**RS\_0** unknown/not necessary  
**AGS\_0** unknown/not necessary  
**WSK** unknown/not necessary  
**EWZ** (numeric) Population

**KFL** (numeric) Area in sq. km  
**DEBKG\_ID** unknown/not necessary  
**Shape\_\_Are** unknown/not necessary  
**Shape\_\_Len** unknown/not necessary  
**death\_rate**  
**cases** (numeric) COVID-19 cases  
**deaths** (numeric) COVID-19 associated deaths  
**cases\_per\_** (numeric) COVID-19 cases per 100,000 inhabitants  
**cases\_pe\_1** unknown/not necessary  
**BL** (character) Federal state  
**BL\_ID** (integer) Federal state ID  
**county** (character) County name  
**last\_updat** Date of last update  
**geometry** Geometry

### Details

The data is included as it was published in by the Robert Koch Institute (Robert Koch-Institut, RKI) but extended by the geometry column (Original data: shapefile).

### Source

RKI (2020) RKI Corona Landkreise. Robert Koch-Institut (RKI), dl-de/by-2-0. Attribution: Robert Koch-Institut, Bundesamt für Kartographie und Geodäsie. <https://npgeo-corona-npgeo-de.hub.arcgis.com/datasets/917fc37a7095> (retrieved 2020-03-30)

### Examples

```

data(RKI_Corona_counties)
# German counties (Source: Robert Koch Institute)

Corona_nbstat <-
  nbstat (
    RKI_Corona_counties,
    ID_col="AGS",
    link_data = RKI_Corona_counties,
    data_ID_col = "AGS",
    data_col = "EWZ",
    func = "sum"
  )
Corona_nbstat$nbmat_data_aggregate
# Sum of population (EWZ) of neighbouring counties

```

R\_t

*Effective Reproduction Number for Epidemic Data***Description**

Calculation of the effective reproduction number for infection/surveillance data

**Usage**

```
R_t(
  infections,
  GP = 4,
  correction = FALSE
)
```

**Arguments**

infections	numeric vector with infection data
GP	Generation period, in days
correction	Correction of values equal to zero? (Recommended)

**Details**

The function calculates the effective reproduction number (=growth factor),  $R_t$ , of an infections time series.

**Value**

list with two entries:

R_t:	Object of class "numeric" $R_t$ values
infections_data:	Object of class "data.frame" Dataset with infections data and $R_t$

**Author(s)**

Thomas Wieland

**References**

Bonifazi G et al. (2021) A simplified estimate of the effective reproduction number  $R_t$  using its relation with the doubling time and application to Italian COVID-19 data. *The European Physical Journal Plus* 136, 386. doi:10.1140/epjp/s13360021013396

Wieland T (2020) A phenomenological approach to assessing the effectiveness of COVID-19 related nonpharmaceutical interventions in Germany. *Safety Science* 131, 104924. doi:10.1016/j.ssci.2020.104924

**See Also**

[logistic\\_growth](#)

**Examples**

```
data(COVID19Cases_geoRegion)
# Get SWISS COVID19 cases at NUTS 3 level

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[!COVID19Cases_geoRegion$geoRegion %in% c("CH", "CHFL"),]
# Exclude CH = Switzerland total and CHFL = Switzerland and Liechtenstein total

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[COVID19Cases_geoRegion$datum <= "2020-05-31",]
# Extract first COVID-19 wave

COVID19Cases_BS <-
  COVID19Cases_geoRegion[(COVID19Cases_geoRegion$geoRegion == "ZH")
    & (COVID19Cases_geoRegion$sumTotal > 0),]
# COVID cases for Zurich

Rt_BS <- R_t(infections = COVID19Cases_BS$entries)
# Effective reproduction number

Rt_BS
```

---

sbm-class

*Class "sbm"*


---

**Description**

The class "sbm" contains the results of the Swash-Backwash Model and the related input data as well as additional information. Use `summary(sbm)` and `plot(sbm)` for results summary and plotting, respectively.

**Objects from the Class**

Objects can be created by the function `swash`.

**Slots**

**R\_0A:** Object of class "numeric" Model result: spatial reproduction number  $R_{0A}$   
**integrals:** Object of class "numeric" Model result: integrals  $S_A$ ,  $I_A$ , and  $R_A$   
**velocity:** Object of class "numeric" Model result: velocity measures  $t_{FE}$  and  $t_{LE}$   
**occ\_regions:** Object of class "data.frame" Model result: Occurence at regional level  
**SIR\_regions:** Object of class "data.frame" Model result: Susceptible, infected and recovered regions over time

**cases\_by\_date:** Object of class "data.frame" Total cases by date  
**cases\_by\_region:** Object of class "data.frame" Cumulative cases by region  
**input\_data:** Object of class "data.frame" Input data  
**data\_statistics:** Object of class "numeric" Diagnostics of input data  
**col\_names:** Object of class "character" Original column names in input data

## Methods

**confint** signature(object = "sbm"): Creates bootstrap confidence intervals for sbm objects.  
**plot** signature(x = "sbm"): Plots the results of the Swash-Backwash Model; two plots: edges over time, total infections per time unit  
**print** signature(x = "sbm"): Prints an sbm object; use summary(sbm) for results  
**show** signature(object = "sbm"): Prints an sbm object; use summary(sbm) for results  
**summary** signature(object = "sbm"): Prints a summary of sbm objects (results of the Swash-Backwash Model)  
**growth** signature(object = "sbm"): Estimates logistic growth models from sbm objects  
**growth\_initial** signature(object = "sbm"): Estimates exponential growth models from sbm objects for a given time period

## Author(s)

Thomas Wieland

## References

Chowell G, Viboud C, Hyman JM, Simonsen L (2015) The Western Africa ebola virus disease epidemic exhibits both global exponential and local polynomial growth rates. *PLOS Currents Outbreaks*, ecurrents.outbreaks.8b55f4bad99ac5c5db3663e916803261. doi:10.1371/currents.outbreaks.8b55f4bad99ac5c5db3663e916803261  
 Cliff AD, Haggett P (2006) A swash-backwash model of the single epidemic wave. *Journal of Geographical Systems* 8(3), 227-252. doi:10.1007/s1010900600278  
 Smallman-Raynor MR, Cliff AD, Stickler PJ (2022) Meningococcal Meningitis and Coal Mining in Provincial England: Geographical Perspectives on a Major Epidemic, 1929–33. *Geographical Analysis* 54, 197–216. doi:10.1111/gean.12272  
 Smallman-Raynor MR, Cliff AD, The COVID-19 Genomics UK (COG-UK) Consortium (2022) Spatial growth rate of emerging SARS-CoV-2 lineages in England, September 2020–December 2021. *Epidemiology and Infection* 150, e145. doi:10.1017/S0950268822001285.  
 Wieland T (2020) Flatten the Curve! Modeling SARS-CoV-2/COVID-19 Growth in Germany at the County Level. *REGION* 7(2), 43–83. doi:10.18335/region.v7i2.324

## Examples

```
showClass("sbm")
```

sbm\_ci-class

Class "sbm\_ci"

## Description

The class "sbm\_ci" contains the results of the Swash-Backwash Model, confidence intervals for the model estimates, and the related input data as well as additional information. Use `summary(sbm_ci)` and `plot(sbm_ci)` for results summary and plotting, respectively.

## Objects from the Class

Objects can be created by the function `confint(sbm)`.

## Slots

**R\_0A:** Object of class "numeric" Model result: spatial reproduction number  $R_{0A}$   
**integrals:** Object of class "numeric" Model result: integrals  $S_A$ ,  $I_A$ , and  $R_A$   
**velocity:** Object of class "numeric" Model result: velocity measures  $t_{FE}$  and  $t_{LE}$   
**occ\_regions:** Object of class "data.frame" Model result: Occurence at regional level  
**cases\_by\_date:** Object of class "data.frame" Total cases by date  
**cases\_by\_region:** Object of class "data.frame" Cumulative cases by region  
**input\_data:** Object of class "data.frame" Input data  
**data\_statistics:** Object of class "numeric" Diagnostics of input data  
**col\_names:** Object of class "character" Column names in input data  
**integrals\_ci:** Object of class "list" Confidence intervals for integrals  $S_A$ ,  $I_A$ , and  $R_A$   
**velocity\_ci:** Object of class "list" Confidence intervals for velocity measures  $t_{FE}$  and  $t_{LE}$   
**R\_0A\_ci:** Object of class "numeric" Confidence intervals for spatial reproduction number  $R_{0A}$   
**iterations:** Object of class "data.frame" Results of bootstrap sampling iterations  
**ci:** Object of class "numeric" Lower and upper confidence intervals based on user input  
**config:** Object of class "list" Configuration details for bootstrap sampling

## Methods

**plot** signature(x = "sbm\_ci"): Plots the results of bootstrap confidence intervals for the Swash-Backwash Model; one figure with six plots:  $S_A$ ,  $I_A$ ,  $R_A$ ,  $t_{FE}$ ,  $t_{LE}$ , and  $R_{0A}$   
**print** signature(x = "sbm\_ci"): Prints an sbm\_ci object; use `summary(sbm_ci)` for results  
**show** signature(object = "sbm\_ci"): Prints an sbm\_ci object; use `summary(sbm_ci)` for results  
**summary** signature(object = "sbm\_ci"): Prints a summary of sbm\_ci objects (bootstrap confidence intervals for Swash-Backwash Model estimates)



**Author(s)**

Thomas Wieland

**References**

*Swash-Backwash Model:*

Cliff AD, Haggett P (2006) A swash-backwash model of the single epidemic wave. *Journal of Geographical Systems* 8(3), 227–252. doi:10.1007/s1010900600278

Smallman-Raynor MR, Cliff AD, Stickler PJ (2022) Meningococcal Meningitis and Coal Mining in Provincial England: Geographical Perspectives on a Major Epidemic, 1929–33. *Geographical Analysis* 54, 197–216. doi:10.1111/gean.12272

Smallman-Raynor MR, Cliff AD, The COVID-19 Genomics UK (COG-UK) Consortium (2022) Spatial growth rate of emerging SARS-CoV-2 lineages in England, September 2020–December 2021. *Epidemiology and Infection* 150, e145. doi:10.1017/S0950268822001285.

*Bootstrapping und bootstrap confidence intervals:*

Efron B, Tibshirani RJ (1993) An Introduction to the Bootstrap.

Ramachandran KM, Tsokos CP (2021) Mathematical Statistics with Applications in R (Third Edition). Ch. 13.3.1 (Bootstrap confidence intervals). doi:10.1016/B9780128178157.000130

**Examples**

```
showClass("sbm_ci")
```

---

show-methods

*Methods for Function show*

---

**Description**

Methods for function show

**Methods**

signature(object = "sbm") Prints an sbm object; use summary(sbm) for results

signature(object = "sbm\_ci") Prints an sbm\_ci object; use summary(sbm\_ci) for results

---

summary-methods	<i>Methods for Function summary</i>
-----------------	-------------------------------------

---

## Description

Methods for function summary

## Methods

`signature(object = "sbm")` Prints a summary of sbm objects (results of the Swash-Backwash Model)

`signature(object = "sbm_ci")` Prints a summary of sbm\_ci objects (bootstrap confidence intervals for Swash-Backwash Model estimates)

`signature(object = "countries")` Prints a summary of a countries object built with the function [compare\\_countries](#)

---

swash	<i>Swash-Backwash Model for the Single Epidemic Wave</i>
-------	--

---

## Description

Analysis of regional infection/surveillance data using the Swash-Backwash Model for the single epidemic wave by Cliff and Haggett (2006)

## Usage

```
swash(
  data,
  col_cases,
  col_date,
  col_region
)
```

## Arguments

<code>data</code>	<code>data.frame</code> with regional infection data
<code>col_cases</code>	Column containing the cases (numeric)
<code>col_date</code>	Column containing the time points (e.g., days)
<code>col_region</code>	Column containing the unique identifier of the regions (e.g., name, NUTS 3 code)

## Details

The function performs the analysis of the input panel data using the Swash-Backwash Model. The output is an object of class "sbm". The results can be viewed using `summary(sbm)`. The user must state panel data with daily infections.

## Value

object of class `sbm-class`

## Author(s)

Thomas Wieland

## References

Cliff AD, Haggett P (2006) A swash-backwash model of the single epidemic wave. *Journal of Geographical Systems* 8(3), 227-252. doi:[10.1007/s1010900600278](https://doi.org/10.1007/s1010900600278)

Smallman-Raynor MR, Cliff AD, Stickler PJ (2022) Meningococcal Meningitis and Coal Mining in Provincial England: Geographical Perspectives on a Major Epidemic, 1929–33. *Geographical Analysis* 54, 197–216. doi:[10.1111/gean.12272](https://doi.org/10.1111/gean.12272)

Smallman-Raynor MR, Cliff AD, The COVID-19 Genomics UK (COG-UK) Consortium (2022) Spatial growth rate of emerging SARS-CoV-2 lineages in England, September 2020–December 2021. *Epidemiology and Infection* 150, e145. doi:[10.1017/S0950268822001285](https://doi.org/10.1017/S0950268822001285).

## See Also

`sbm-class`

## Examples

```
data(COVID19Cases_geoRegion)
# Get SWISS COVID19 cases at NUTS 3 level

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[!COVID19Cases_geoRegion$geoRegion %in% c("CH", "CHFL"),]
# Exclude CH = Switzerland total and CHFL = Switzerland and Liechtenstein total

COVID19Cases_geoRegion <-
  COVID19Cases_geoRegion[COVID19Cases_geoRegion$datum <= "2020-05-31",]
# Extract first COVID-19 wave

CH_covidwave1 <-
  swash (
    data = COVID19Cases_geoRegion,
    col_cases = "entries",
    col_date = "datum",
    col_region = "geoRegion"
  )
# Swash-Backwash Model for Swiss COVID19 cases
# Spatial aggregate: NUTS 3 (cantons)
```

```
summary(CH_covidwave1)
# Summary of Swash-Backwash Model

plot(CH_covidwave1)
# Plot of Swash-Backwash Model edges and total epidemic curve
```

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